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# **Fuzzy Temporal Non-monotonic Reasoning**

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### **Abstract**

Non-monotonic reasoning is different kind of reasoning in which many conclusions drawn by adding knowledge. Temporal non-monotonic reasoning in which conclusion will be changed when time goes on changed. For instance, the bird can't fly up to certain age. The non-monotonic problem is undecided. An undecided problem has no solution. Fuzzy logic will made undecided problem into decidable problem. In this paper, on-monotonic reasoning is studied with fuzzy temporal constraints to get better conclusion. Fuzzy temporal truth maintenance system (FTTMS) is studied to arrive at conclusion for non-monotonic reasoning.

**Keywords:** non-monotonic reasoning, fuzzy Sets, twofold fuzzy sets, fuzzy non-monotonic reasoning, FTTMS, incomplete knowledge

# I. INTRODUCTION

Non-monotonic reasoning will draw different conclusions and it is undecided reasoning. Sometimes Artificial Intelligence (AI) has to deal with undecided problems. Non-monotonic problem is undecided. In non.-monotonic reasoning, if some knowledge is added to the system then the conclusion will be changed, if knowledge base is incomplete then the

reasoning is also incomplete. Knowledge bases are collecting the facts and give the conclusion based on facts. If the knowledge is temporal; then the reasoning also changes. For instance, a young bird is kept in room. After sometime it is escaped. Whether the bird can fly or not? Here age of the bird is involved.

John McCarthy [5] formalized non-monotonic reasoning with predicates P(x1,x2,...,xn) for the propositions of type "x is A".

The non-monotonic logic may be defined as

 $\forall x (P(x) \land Q(x) \rightarrow R(x))$ 

 $\exists P(x) \land Q(x) \rightarrow \neg R(x)$ 

For instance,

 $\forall x (bird(x) \land wings(x) \rightarrow fly(x))$ 

bird(peacock)  $\land$  wings(peacock)  $\rightarrow$  fly(peacock)

 $\exists x (bird(x) \land wings(x) \rightarrow f) \rightarrow fly(x))$ 

 $\exists x \text{ (bird(penguin) } \Lambda \text{ wings(penguin) } \rightarrow_{\mathsf{T}} \text{fly(penguin))}$ 

The temporal logic is logic with time constraints and Time variables "t1-t0" like "before", "meet", "after", where starting time t0 and ending time t1. The time constraints are necessary to deal with data [1, 4].

Sometimes temporal logic may con FL2n incomplete information of time constraints. Fuzzy will deal with incomplete information.

Fuzzy temporal proposition is of the form "x" is  $\tilde{A}$ ", where  $\tilde{A}$  is temporal fuzzy set.

Definition: A temporal set  $\tilde{A}$  is characterized by its membership function  $\mu_{\tilde{A}}(t)$ , where  $t=t_e-t_s$ ,  $t_s$  is starting time and  $t_e$  ending time and  $t1>t_0$ 

For instance

past=ts>t<sub>e</sub>

Present=t<sub>e</sub>=t<sub>s</sub>

feature=ts<te

latte=ts>te

in time=t<sub>e</sub>=t<sub>s</sub>

early=ts<te

For instance,

late= 
$$\mu_{late}(t)/t = \mu_{late}(t1)/t1 + ... + \mu_{late}(tn)/tn$$

For instance,

The fuzzy proposition may con FL2n time variables like.

"x is early"

"x is late"

Late=0/1+0.1/10+0.3/20+0.6/30+0.8/40+1.0/50+1/60

early=0.1/5+0.3/20+0.6/30+0.8/40+0.9/50+1/60

fly-age=0.0/5+0.3/20+0.6/30+0.8/40+0.9/50+1/60

at the age of 5 days, the bird can't fly but at age of 20 days, the bird can fly.

#### I. FUZZY LOGIC

Zadeh [15] fuzzy logic is based on belief rather than probable (likelihood). The fuzzy logic made imprecise information in to precise.

Zadeh fuzzy logic is characterized by single membership function.

Zadeh[16] has introduced fuzzy set as a model to deal with incomplete information. Fuzzy set is a class of objects with a continuum of grades.

The set A of X is characterized by its membership function  $\mu_A(x)$  and ranging values in the unit interval [0,1]

 $\mu_A(x)$ : X  $\rightarrow$  [0, 1], x  $\in$  X, where X is Universe of discourse.

$$A = \mu_A(x_1)/x_1 + \mu_A(x_2)/x_2 + ... + \mu_A(a_n)/x_n$$
, where "+" is union

 $\mu_{\text{bird}}(x) = \mu_{\text{bird}}(x_1)/x_1 + \mu_{\text{bird}}(x_2)/x_2 + ... + \mu_{\text{bird}}(x_n)/x_n$ 

 $\mu_{bird}(x) = \mu_{bird}(x_1)/x_1 + \mu_{bird}(x_2)/x_2 + ... + \mu_{bird}(x_n)/x_n$ 

 $\mu_{bird}(x) = 0.1/Penguin + 0.3/Hen + 0.5/Cock + 0.6/Parrot + 0.8/eagle + 1.0/flamingos$ 

 $\mu_{A}(x)=1-\mu_{A}(x)$  Negation

 $\mu_A(x)\Lambda\mu_A(x) = \min\{\mu_A(x)\Lambda,\mu_A(x)\}$  Conjunction

 $\mu_A(x)V\mu_A(x) = \max \{\mu_A(x), \mu_A(x)\}$  Disjunction

$$\mu_{QA}(x) = \mu_A(x)^q$$

Quantifier

The fuzzy rules are of the form "if <Precedent Part> then <Consequent Part>"

if x is P the n x is Q.

.if x is  $P_1$  and x is  $P_2$  .... x is  $P_n$  then x is Q

The Zadeh [14] fuzzy conditional inference s given by

if x is 
$$P_1$$
 and x is  $P_2$  .... x is  $P_n$  then x is  $Q = \min 1$ ,  $(1-\min(\mu_{P_1}(x), \mu_{P_2}(x), ..., \mu_{P_n}(x)) + \mu_Q(x)$  (2.1)

The Mamdani [8] fuzzy conditional inference s given by

if x is 
$$P_1$$
 and x is  $P_2$  .... x is  $P_n$  then x is  $Q = \min \{ \mu_{P1}(x), \mu_{P2}(x), ..., \mu_{Pn}(x), \mu_{Q}(x) \}$  (2.2)

The fuzzy conditional inference may be derived "Consequent Part" from "Precedent Part". [15].

Fuzzy conditional inference is given by fuzzy conditional inference

If x is then x is  $Q = {\mu_P(x)}$ 

 $if \quad x \ is \ P_1 \ and \quad x \ is \ P_2... \ x \quad is \ P_n \ then \quad x \ is \ Q$ 

={  $\min(\mu_{P1}(x), \mu_{P2}(x), ..., \mu_{Pn}(x),)$ } (2.3).

$$P(x) \land Q(x) \rightarrow R(x) = \{P(x) \land Q(x)\}\$$

For instance,

x is bird  $\Lambda$  x has wings  $\rightarrow$  x can fly

=x is bird  $\Lambda$  x has wings

# II. FUZZY TEMPORAL NON-MONOTONIC REASONING

The temporal logic is logic with time constraints and Time variables "t1-t0" like "before", "meet", "after", where starting time t0 and ending time t1.

The time constraints are necessary to deal with data [1, 4]. Fuzzy temporal logic should deal with incomplete information of time constraints.

A temporal variable is " $t_1$ - $t_0$ ", where t0 is starting time and t1 ending time.

For instance "past"= $t_1$ - $t_0$ ,  $t_1$ < $t_0$ 

"Present" =  $t_1$  approximately  $t_0$ 

"feature"= $t_1$ - $t_0$ ,  $t_1$ > $t_0$ 

A fuzzy temporal set is fuzzy set of temporal constraint.

Fuzzy Temporal non-monotonic reasoning May be formalized with fuzzy predicate for the proposition of type "x is A", when A is fuzzy set may be defined as

 $\forall x (P(x) \land T(x) \rightarrow R(x))$ 

 $\forall x (P(x) \land T(x) \rightarrow R(x))$ 

For instance,

 $\forall x (bird(x) \land young(x) \rightarrow fly(x))$ 

 $\forall x (bird(x) \land young(x) \rightarrow \neg fly(x)$ 

x is bird  $\Lambda$  x is young  $\Lambda$  x is unknown to fly  $\rightarrow$ x can fly

Suppose,

x is bird  $\Lambda$  x is young  $\Lambda$  x is unknown to fly  $\rightarrow$ x can 't fly

or

x is bird $\Lambda$  x is young  $\Lambda$  x is unknown to fly  $\rightarrow$ x can't fly

For example,

Ozzie is bird $\Lambda$ Ozzie is young  $\Lambda$ Ozzie is unknown to fly  $\rightarrow$ Ozzie can fly

Ozzie is birdΛOzzie is young ΛOzzie is known to fly →Ozzie can't fly

Ozzie is bird∧Ozzie is young ∧Ozzie is unknown to fly →Ozzie can fly

The fuzzy temporal non-monotonic logic may be defined as

 $\forall x (P(x) \land Q(x) \land T(x) \land R(x) \rightarrow S(x))$ 

 $\forall x (P(x) \land Q(x) \land T(x) \land R(x) \rightarrow_{7} S(x)$ 

For instance,

 $\forall x (bird(x) \land wings(x) \land young(x) \land unknown-of-fly(x) \rightarrow fly(x))$ 

 $\forall x (bird(x) \land wings(x) \land young(x) \land known-of-fly(x) \rightarrow_{\neg} fly(x)$ 

#### III. GENERALIZED FUZZY TEMPORAL NON-MONOTONIC REASONING

Zadeh [13] Proposed fuzzy set with single membership function. The two fold fuzzy set [12] will give more evidence than single membership function.

The fuzzy non-monotonic set may defined with two fold membership function using unknown and known

**Definition**: Given some Universe of discourse X, the proposition "x is P" is defined as its two fold fuzzy membership function as

$$\mu_P(x) = \{\mu_P^{known}(x), \mu^{unknown}(x)\}$$

$$P = \{\mu_P^{known}(x), \mu_P^{unknown}(x)\}$$

Where P is Generalized fuzzy set and  $x \in X$ ,

$$u_P(x)^{(known, unknown)} \Lambda u_O(x)^{(known-, unknown)} \rightarrow u_S(x)^{(known, unknown)}$$

where P,Q and S are twofold fuzzy sets with [known, unknown].

$$\mu_{bird}(x) \wedge \mu_{wings}(x) \rightarrow \mu_{fly}(x)$$

$$\mu_{bird}(x)^{(known,unknown)} \Lambda \mu_{wings}(x)^{(known-,unknown)} \rightarrow \mu_{flv}(x)^{(known,unknown)}$$

The conflict of the incomplete information may be defined by fuzzy certainty factor(FCF).

FCF =(known- unknown)

$$\mu^{FCF}_{P}(x) \rightarrow [0,1], x \in X$$

$$\mu_{\text{bird}}^{\text{FCF}}(x) \rightarrow [0,1]$$

Where known and unknown are the fuzzy membership functions.

The fuzzy non-monotonic reasoning will bring uncertain knowledge in to certain knowledge.

$$\mu_{bird}(x)$$
 (known, unknown)  $\rightarrow \mu_{fly}(x)$ 

$$\mu_P(x) \xrightarrow{(known, unknown)} \mu_S(x)$$

$$S = \mu_S^{FCF}(x) = 1 \quad \mu_P^{FCF}(x) = \alpha$$

$$0 \quad \mu_{P}^{FCF}(x) < \alpha$$

fly= 
$$\mu_{\text{fly}}^{\text{FCF}}(x) = 1$$
  $\mu_{\text{bird}}^{\text{FCF}}(x) = 0.56$   
0  $\mu_{\text{bird}}^{\text{FCF}}(x) < 0.5$ 

```
{0.2/penguin +0.3/Ozzie+ 0.8/parrot+ 0.9/waterfowl + 1.0/eagle , 0.1/penguin
+0.2/Ozzie+ . 0.1/parrot+ 0.1/waterfowl + 0.1/eagle }
Wings= {0.1/penguin +0.3/Ozzie+ 0.7/parrot+ 0.8/waterfowl + 0.9/eagle, 0.0/penguin
+0.1/Ozzie+ . 0.2/parrot+ 0.1/waterfowl + 0.1/eagle }
Definition: The two fold fuzzy set for the proposition of the type "x is P" is given by
\mu_P(x) = \{\mu_P^{known}(x), \mu_P^{unknown}(x)\}
\mu_{\text{bird}}^{\text{FCF}}(x) = \{\mu_{\text{bird}}^{\text{known}}(x), -\mu_{\text{bird}}^{\text{unkown}}(x)\}
= \{0.2/\text{penguin} + 0.3/\text{Ozzie} + 0.8/\text{parrot} + 0.9/\text{waterfowl} + 1.0/\text{eagle}, 0.1/\text{penguin} + 0.1/\text{Ozzie} + ...
0.1/parrot + 0.1/waterfowl + 0.1/eagle
= \{0.1/\text{penguin} + 0.2/\text{Ozzie} + .0.7/\text{parrot} + 0.8/\text{waterfowl} + 0.9/\text{eagle}\}
\mu_{\text{ wings}}^{\text{ FCF}}(x) = \{\mu_{\text{wings}}^{\text{ known}}(x), \text{-} \mu_{\text{wings}}^{\text{ unknown}}(x)\}
wings= {0.1/penguin +0.3/Ozzie+ 0.7/parrot+ 0.8/waterfowl + 0.9/eagle, 0.0/penguin
+0.1/Ozzie+ . 0.2/parrot+ 0.1/waterfowl + 0.1/eagle }
= \{ 0.1/\text{penguin} + 0.2/\text{Ozzie} + .0.5/\text{parrot} + 0.6/\text{waterfowl} + 0.8/\text{eagle} \}
\mu_{\text{young}}^{\text{FCF}}(x) = \{\mu_{\text{wings}}^{\text{known}}(x), -\mu_{\text{wings}}^{\text{unknown}}(x)\}
young= {0.3/penguin +0.4/Ozzie+ 0.7/parrot+ 0.8/waterfowl + 0.9/eagle, 0.0/penguin
+0.1/Ozzie+ . 0.2/parrot+ 0.3/waterfowl + 0.3/eagle }
= = { 0.3/penguin +0.4/Ozzie+ . 0.3/parrot+ 0.5/waterfowl + 0.6/eagle }
Using (2.3), fuzzy inference is given by
if x is P_1 and x is P_2 .... x is P_n then x is Q
if x 	ext{ is } P_1 	ext{ and } x 	ext{ is } P_2 	ext{ .... } x 	ext{ is } P_n 	ext{then } x 	ext{ is } Q_1
Q_1 = P_1 \Lambda P_2 \Lambda \dots \Lambda P_n
The fuzzy temporal non-monotonic logic may be defined as
\forall x (P(x) \land Q(x) \land T(x) \land R(x) \rightarrow S(x))
\forall x (P(x) \land Q(x) \land T(x) \land R(x) \rightarrow_{\neg} S(x)
For instance,
\forall x (bird(x) \land wings(x) \land young(x) \land unknown-of-fly(x) \rightarrow fly(x))
```

 $\forall x (bird(x) \land wings(x) \land young(x) \land known-of-fly(x) \rightarrow_{\neg} fly(x)$ 

The two statements combined with two fold fuzzy logic.

x is bird $\Lambda$  x has wings $\Lambda$  x is young  $\rightarrow$  x can fly

x can fly=x is bird  $\Lambda$  x is young  $\Lambda$  x has wings

$$\mu_{\text{bird}}(x) \wedge \mu_{\text{wings}}(x) \wedge \mu_{\text{young}}(x) \rightarrow \mu_{\text{fly}}(x)$$

 $\{\mu_{\text{bird}} \text{ known } (x), \ \mu_{\text{bird}} \text{ unknown } (x)\} \Lambda \{ \ \mu_{\text{bird}} \text{ known } (x), \ \mu_{\text{bird}} \text{ unknown } (x)\} \Lambda \{ \ \mu_{\text{young}} \text{ known } (x), \ \mu_{\text{young}} \text{ unknown } (x)\} = \mu_{\text{flv}}(x)$ 

$$\mu_{\text{bird}}$$
 FCF(x)  $\Lambda \mu_{\text{wings}}$  FCF(x) $\Lambda \mu_{\text{youngs}}$  FCF(x) $\rightarrow \mu_{\text{fly}}$ (x)

if x is  $P_1$  and  $P_2$  ...x is  $P_n$  then x is  $P_1$  and  $P_2$  .... x is  $P_n$ 

= 
$$min(\mu_{P1}(x), \mu_{P2}(x), ..., \mu_{Pn}(x))$$

$$\mu_{fly}(x) = \mu_{bird}^{FCF}(x) \Lambda \mu_{wings}^{FCF}(x)$$

$$\mu_{bird}^{FCF}(x) = \{0.1/penguin + 0.1/Ozzie + .0.7/parrot + 0.8/waterfowl + 0.9/eagle \}$$

$$\mu_{wings} \text{ FCF}(x) \quad \mu_{wings}(x) \ = \ \{\mu_{wings} \text{ known}(x), \ \mu_{wings} \text{ unknown}(x)\}$$

=  $\{0.1/\text{penguin} + 0.2/\text{Ozzie} + .0.5/\text{parrot} + 0.6/\text{waterfowl} + 0.8/\text{eagle}\}$ 

$$\mu_{young}^{FCF}(x) = {\mu_{young}^{known}(x), \mu_{youngs}^{unknown}(x)}$$

= 
$$\{0.3/\text{penguin} + 0.4/\text{Ozzie} + .0.3/\text{parrot} + 0.5/\text{waterfowl} + 0.6/\text{eagle}\}$$

Fuzzy conditional inference "consequent part "may be derived from "precedent part".

x is bird  $\Lambda$  x has wings  $\Lambda$  x is young  $\rightarrow$  x can fly

x can fly =min { x is bird, x has wings}

= 
$$\{0.1/\text{penguin} + 0.2/\text{Ozzie} + .0.3/\text{parrot} + 0.5/\text{waterfowl} + 0.6/\text{eagle}\}$$

The inference of "x can fly" for  $\alpha >=0.5$  is given by

= 1/waterfowl + 1/eagle

Here fuzzy logic made incomplete information to precise information's. Some birds can fly and some birds can't fly.

The fuzzy decision sets or quasi fuzzy set is defined by

$$R = \mu_A^R(x) = 1 \quad \mu_A^{FCF}(x) > = \alpha,$$

$$0 \quad \mu_A^{FCF}(x) < \alpha$$

The parrot, waterfowl and eagle can fly.

The penguin and Ozzie can't fly

The inference of "x can't fly" for  $\alpha$ <0.5 is given by

= 0/.1penguin +0.2/Ozzie

The inference of "x can fly" for  $\alpha \ge 0.5$  is given by

= 0.6/parrot + 0.6/waterfowl + 0.8/eagle

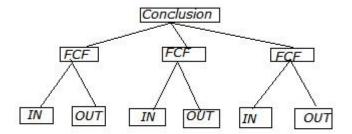
he parrot, waterfowl and eagle can fly and, penguin and Ozzie are can't fly.

#### IV. FUZZY TEMPORAL TRUTH MAINTEANANCE SYSTEM

Doyel [4] studied truth maintenance system TMS for non-monotonic reasoning

The fuzzy truth maintenance system (FTTMS) for fuzzy non-monotonic reasoning using fuzzy conditional inference as

FTTMS is having There is list of justification and conditions.



Fuzzy Temporal Truth Maintenance System

if x is bird and x has wings and x is young x is fly-age then x can fly

List L(IN-node, OUT-node), FCF-node

IN-node is known

OUT-node is unknown

FCF is (belirf-disbilief)

Consider the proposition "if x is bird then x can fly)

x is bird

IN 0.9

**OUT 0.1** 

FCF 0.8

Conclusion : x can fly if FCF>=0.5.

x is bird IN 0.3 OUT 0.1 FCF 0.2 Conclusion:x can't fly if FCF<0.5. Consider the proposition "if x has wings then x is fly) x has wings IN 0.8 **OUT 0.1** FCF 0.7 Conclusion : x can fly if FCF $\ge$ 0.5. x has wings IN 0.3 OUT 0.1 FCF 0.2 Conclusion :x can't flyif FCF<0.5. Consider the proposition " if x is young then x is fly) X is young IN 0.6 OUT 0.1 FCF 0.5 Conclusion: x can fly if FCF>=0.5. x is young IN 0.5 OUT 0.1

FCF 0.4

Conclusion:x can't fly if FCF<0.5. Consider the proposition " if x is fly-age then x is fly) X is fly-age IN 0.8 OUT 0.2 FCF 0.6 Conclusion: x can fly if FTCF>=0.5. x is fly-age IN 0.4 OUT 0.1 FCF 0.3 Conclusion:x can't fly if FTCF<0.5. Where FTCF is Fuzzy Temporal Certainty Factor Consider the proposition "if x is bird and x has wings and x is young and x is fly-age then x is fly) x is bird IN 0.9 OUT 0.1 FCF1 0.8 x has wings IN 0.8 OUT 0.1 FCF2 0.7 X is young IN 0.6 **OUT 0.1** 

FCF3 0.5

X is fly-age

IN 0.8

**OUT 0.2** 

**FTCF 0.6** 

FCF=min{FCF1,FCF2, FCF3, FTCF4}=0.5

Conclusion : x can fly if FCF>=0.5.

Here is the fuzzy temporal no monotonic logic is making imprecise to precise.

#### V. CONCLUSION

Non-monotonic reasoning will give different concussions if some knowledge is added to the theory. Sometimes conclusion will be changed if time goes Fuzzy non-monotonic logic made imprecise to precise. A sometimes time constraint has to deal by fuzzy non-monotonic reasoning. A bird can't fly in the past but it can fly present and it can 'fly feature We discussed the difference between fuzzy temporal fuzzy non-monotonic reasoning and fuzzy monotonic reasoning..

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